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**RELATIONSHIP BETWEEN SHEHU TRANSFORM WITH SOME OTHER INTEGRAL TRANSFORM**

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***ABSTRACT***

*Integral transformations have been successfully used for almost two centuries in solving many problems in applied mathematics, mathematical physics, and engineering science. Shehu transform is new integral transform type which is convenient mathematical methods for solving advance problems of engineering and sciences which are mathematically expressed in terms of differential equations, system of differential equations, partial differential equations, integral equations, system of integral equations, partial integro-differential equations and integro differential equations. In this study, we discussed the relationship between this new integral transform with other some integral transforms.*

***KEYWORDS:*** *Shehu Transform, ZZ Transform, Mohand Transform, Laplace Transform, Sawi Transform, Mahgoub Transform*

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**INTRODUCTION**

Many problems in engineering and science can be formulated in terms of differential equations. The ordinary differential equations arise in many areas of Mathematics, as well as in Sciences and Engineering. In order to solve the certain ordinary differential equations integral transforms are widely used. In this article we have construct the relation between Shehu transform and some other integral transforms which helps us to use Shehu transform simply in solving differential equations.

**SHEHU TRANSFORM**

**Definition:** A new transform called the Shehu transform of the function belonging to a class , where

Where and is givenby:

(1)

**ZZ TRANSFORM**

Let be a function defined for all The ZZ transform of is the function defined by:

(2)

**MOHAND TRANSFORM**

Mohand transform of the function is given by:

(3)

**LAPLACE TRANSFORM**

The Laplace transform of the function is given by:

(4)

**MAHGOUB TRANSFORM**

Mahgoub (Laplace-Carson) transform of the function is given by:

(5)

**SAWI TRANSFORM**

Sawi transform of the function is given by:

(6)

**Connection between Shehu Transform and ZZ Transform**

In this section we show that Shehu transform is theoretical dual of ZZ transform and the dual relation is given by the following relation:

**Theorem 1.1:** Let and if the Shehu transform and ZZ transform of are respectively then

(7)

And

(8)

**Proof:** From (2) we have

Let from the above equation we have

Hence the proof is completed

Now, to drive (8), from (1) we have:

Since, from (2)

Hence the proof of (8) is completed

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| **Table 1: The Relationship Between Shehu Transform and Zz Transform On Some Common Functions** | | | |
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**Connection between Shehu Transform and Laplace Transform**

**Theorem 1.2:** Let and if the Shehu transform and Laplace transform of are respectively then

(9)

**Proof:** Since

Put in the above equation, we have

Therefore

Hence the proof is completed

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| **Table 2: The Relationship between Shehu Transform and Laplace Transform of Some Common Functions** | | | |
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**Connection between Shehu Transform and Mohand Transform**

**Theorem 1.3:**Let and if the Shehu transform and Mohand transform of are respectively then

(10)

And

(11)

**Proof:** Since,

Now, if we substitute

But, from in the above equation we have

Hence the proof is completed

Consequently, to drive (1.11)

Now, multiply the above equation by  both sides, we have

Hence the proof is completed.

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| **Table 3: The Relationship between Shehu Transform and Mohand Transform of Some Common Functions** | | | |
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**Connection between Shehu transform and Mahgoub Transform**

**Theorem 1.4:**Let and if the Shehu transform and Mahgoub transform of are respectively then

(12)

And

(13)

**Proof:** From (1.9) we have

Now, if we substitute

Since from (1.9)

Therefore, . Hence, the proof of (12) is completed

Now, multiply the above equation by both sides, we have:

Hence the proof of (13) is completed.

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| **Table 4: The Relationship between Shehu Transform and Mohgoub Transform of Some Common Functions** | | | |
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**Connection between Shehu Transform and Sawi Transform**

**Theorem 1.5:** Let and if the Shehu transform and Sawi transform of are respectively then

**Proof:** From equation (1.6) we have

Now, if we substitute

Hence, the proof is completed.

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| **Table 5: The Relationship between Shehu Transform and Sawi Transform of Some Common Functions** | | | |
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**CONCLUSIONS**

In this paper, we have successfully discussed the relationship between Shehu transform and some other integral transforms. We have also used tabular representation of Shehu transform and some other integral transform on some common functions to show the connection between Shehu transform and some other integral transform namely, ZZ transform, Mohand transform, Laplace transform, Sawi transform, Mahgoub transform.

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